

Perceiving temporal regularity in music

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Introduction

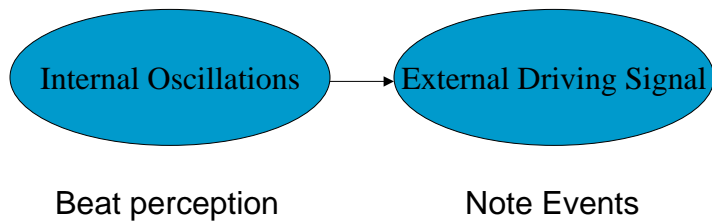
- People have effortless ability to perceive **temporal regularity** in musical sequences.
- Listeners perceive **temporal fluctuations** or deviations as related to performers' musical intentions. (duration-lengthening)





Introduction

- The approach in this paper:
- 1. Model



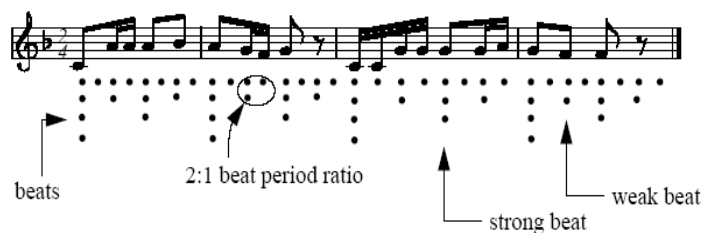
Introduction

- The approach in this paper:
- 2. Experiments
 - a. Evaluate the model's ability to track different temporal periodicities
 - b. Test the model's ability to detect temporal irregularities

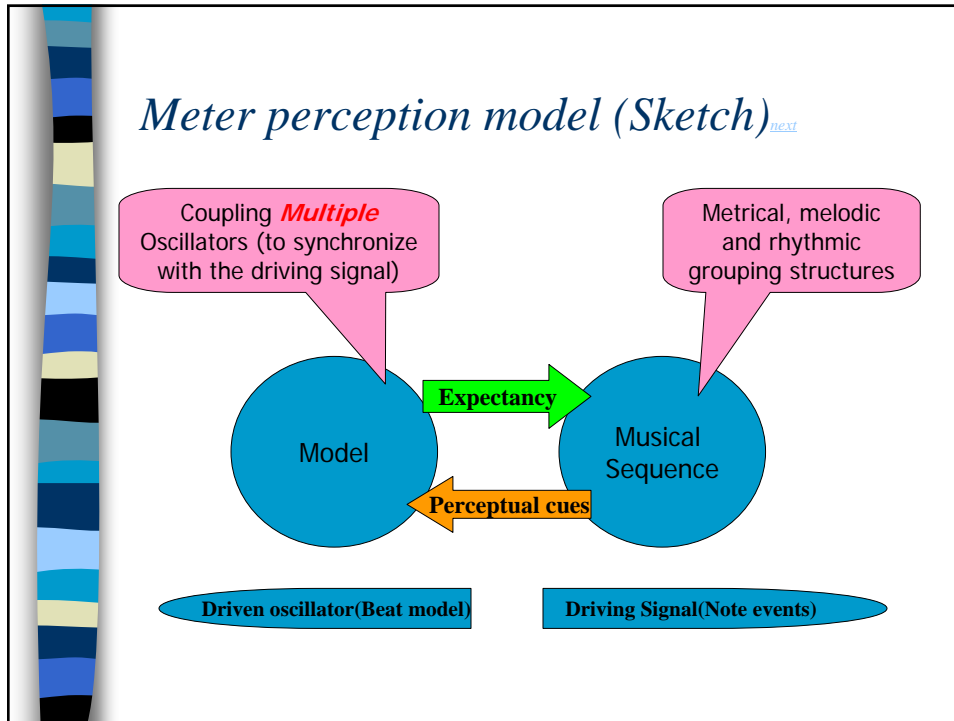
Some basic concepts

- **Rhythm:** the general sense of movement in time, including phrasing, harmony and meter.
- *Temporal patterning of event durations in a sequence*
- **Beat:** pulses marking equally spaced points in time
- *Once it is established, it may continue in mind*
- **Metrical Structure:** alternation of strong and weak beats over time

Strong beats and weak beats



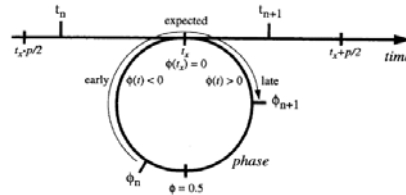
- Strong beats: points at which many beats are coincide
- Weak beats: points at which few beats are coincide
- The first position in the measure is a strong beat
- Inter-onset intervals (IOIs)



- ### Model of single oscillator (prerequisite)
- **Oscillations** are period events (T_0)
 - **Phase** at any time t : $\phi = \frac{t}{T_0}$ (between 0 and 1)
 - **Synchronized**: two oscillations regularly come into phase or begin their cycles together.
 - **Entrainment**: a process by which two or more oscillators achieve synchronization
 - Entrainment occurs because a **coupling** between two or more oscillations causes them to synchronize
 - **Coupling** allows one oscillator to perturb another by altering its **phase**, its **intrinsic period**, or both
 - [Meter perception model \(Sketch\)](#)

Model of single oscillator (prerequisite)

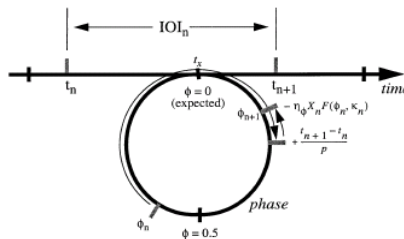
$$\phi_{n+1} = \phi_n + \frac{t_{n+1} - t_n}{p}$$



- Phase of driving oscillator at which the driven oscillator fires on iteration i
- p is the period of driven oscillator
- $\Phi > 0$, event occurred late;
- $\Phi = 0$; corresponds to time of the expected beat;
- $\Phi < 0$; event occurred early;

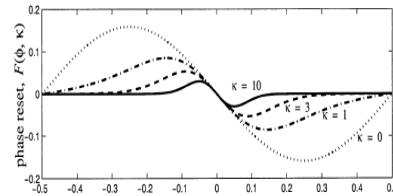
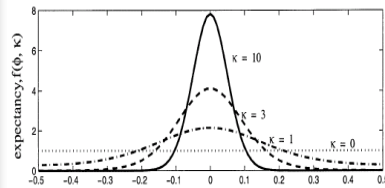
Model of single oscillator

$$\phi_{n+1} = \phi_n + \frac{t_{n+1} - t_n}{p_n} - \eta \phi_n X_n F(\phi_n, \kappa_n) \quad (\text{mod } -0.5, 0.5 \cdot 1)$$



- $F(\Phi, k)$ is the non-linear coupling function;
- X_n is the amplitude of the n th onset ($=1$)
- η is the coupling strength
- k is a focus or concentration parameter that determines the extent of an expectancy function

Expectancy function and Phase resetting function



$$f(\phi, \kappa) = \frac{1}{I_0(\kappa)} \exp \kappa \cos 2\pi\phi$$

$$F(\phi, \kappa) = \frac{1}{2\pi \exp \kappa} [\exp \kappa \cos 2\pi\phi] \sin 2\pi\phi$$

■ Period coupling:

$$p_{n+1} = p_n(1 + \eta_p X_n F(\phi_n, \kappa_n))$$

$$\phi_{n+1} = \phi_n + \frac{t_{n+1} - t_n}{p_n} - \eta_\phi X_n F(\phi_n, \kappa_n) \quad (\text{mod } -0.5, 0.51)$$

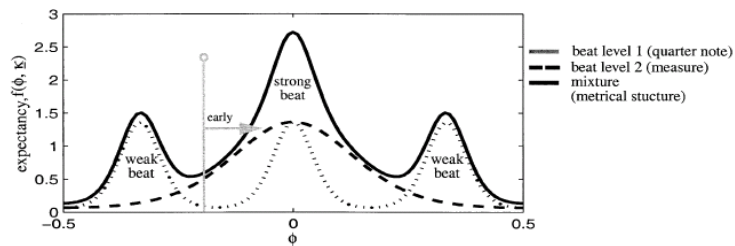
Modeling hierarchical metrical structures (inter-coupling)

- Musical rhythms typically contain multiple periodicities
- The internal oscillators are coupled to one another so as to preserve certain phase and period relationships
- Phase coupling strength α_ϕ
- Period coupling strength α_p

■ Mixture of von Mises distributions

$$f_j(\phi) = \frac{1}{I_0(\kappa_j)} \exp \kappa_j \cos 2\pi j\phi \quad f(\phi, \underline{\kappa}) = \sum_j w_j f_j(\phi)$$

Sensitivity to temporal fluctuations: 1. Categorizing note onsets

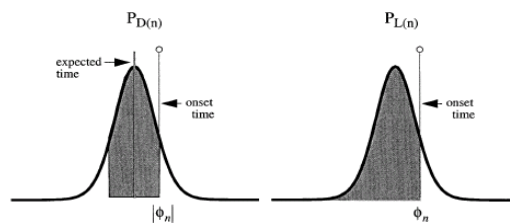


- To find the associated level for ever note event

- Calculation: $f_j(\phi) = \frac{1}{I_0(\kappa_j)} \exp \kappa_j \cos 2\pi_j \phi$

$$f(\phi, \underline{\kappa}) = \sum_j w_j f_j(\phi) \quad \tau_j = \frac{w_j f_j(\phi)}{f(\phi, \underline{\kappa})}$$

Sensitivity to temporal fluctuations: 2. Detecting Phrase-final lengthening



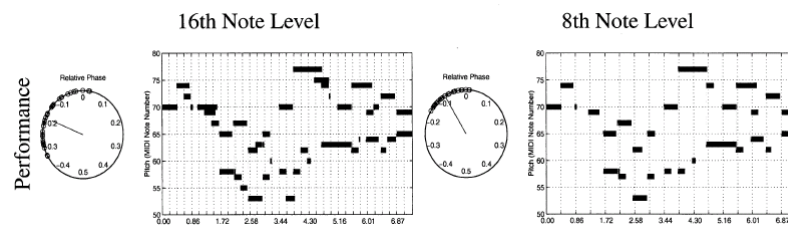
- $P_{D(n)}$: Probability that the event was heard as deviating from its expected time.
- $P_{L(n)}$: Probability that the event was heard as occurring late in the cycle.

$$P_{D(n)} = 2 \int_{x=0}^{|\phi_n|} f(x, \kappa) dx \quad P_{L(n)} = \int_{x=-0.5}^{\phi_n} f(x, \kappa) dx \quad P_{F(n)} = P_{D(n)} P_{L(n)}$$

Experiment (horizontal temporal fluctuations)

- Test sets: Piano performances of 2- and 3-part inventions by Bach.
- 6 players* 4phrase conditions *2 voice entrances *3 excerpts=144 performances
- The simulated oscillations tracked the 16th-note and 8th-note levels of the metrical structure
- Parameters: $p_{16th} = \text{initial IOI} = 1/2 * p_{8th}$;
- $\Phi_0 = 0$; $k=3$; $\eta_\Phi = 1.0$; $\eta_p = 0.4$; $\eta_k = 0.2$
 $\alpha_\Phi = \alpha_p = 1/0$ (coupled/uncoupled)
- Analyzed by circular statistics

Performance timing experiment

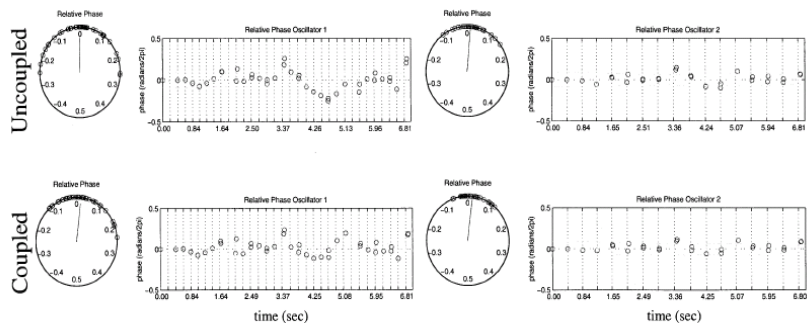


- Performance timing
$$\Phi = \frac{t_{onsettime} - t_{expectedtime}}{p}$$
- $Dev_{16th} > Dev_{8th}$, more expressive timing at the 16th-note level
- Events on and around the notated boundaries had larger relative phase
- Pianists significantly lengthened events at phrase boundaries

Model tracking experiment

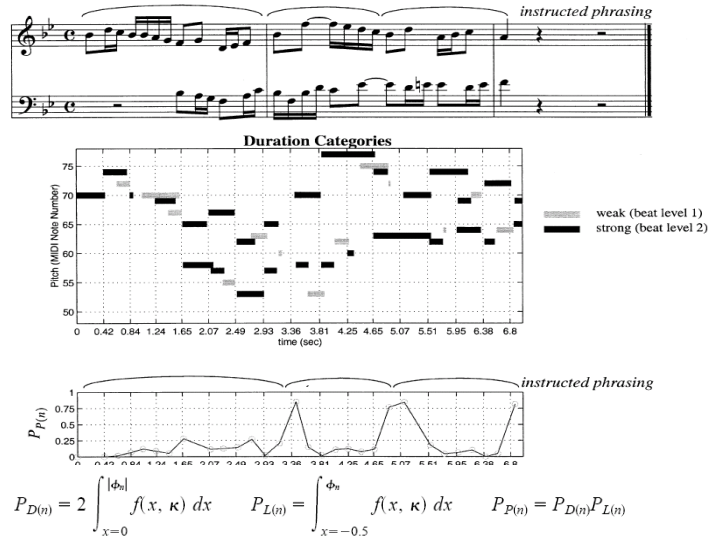
- Phase: $\phi_{n+1} = \phi_n + \frac{t_{n+1} - t_n}{p_n} - \eta_{dr} X_n F(\phi_n, \kappa_n) \pmod{-0.5, 0.51}$
- Angular Dev=0.0801 (smaller than Angular Dev of performance timing)
- ---- *The model adapted phase and period to track the ongoing sequences*
- 1. Different phrase conditions:
 - *The model tracked better in the natural phrase than in the experimental phrase conditions*
- 2. Different metrical level:
 - *The smaller level showed more variability*
- 3. Different voices:
 - *Equally well*

Model tracking experiment



- 4. Coupled and Uncoupled
 - *Tracking by coupled oscillators was better than by the uncoupled oscillators.*
 - *The coupled oscillator model consistently outperformed the uncoupled model, and more so at the smaller metrical level (16th-note)*

Experiment of detecting phrase boundaries



Experiment of detecting phrase boundaries

Table 1
Number of events passing lengthening criterion for performance and model

Model	Performance	
	>75%	<75%
>.75	234 (64%)	120 (12%)
<.75	121 (36%)	935 (88%)

- The model probability of the event >0.75
- The IOI of the event is greater than 75% of all performed events
- Conclusion: the model was able to detect lengthening more often than chance at locations where performers used lengthening



Conclusions

- The model is good
- The first test of a multiple oscillator model tracking music performances
- The model's beat tracking variability was slightly lower than the amount of stimulus variability
- The model detected those events that contained rubato (phrase-final lengthening) well
- The coupling of oscillators improved the model's beat-tracking
- Coupling aided beat-tracking most at metrical levels that contained the most temporal variability.



References

- 1. Glass, L., & Mackey, M. C. (1988). *From clocks to chaos: the rhythms of life*.
- 2. Large, E. W., & Kolen, J. F. (1994). Resonance and the perception of musical meter. *Connection Science*, 6, 177-208
- 3. Large, E. W., & Jones, M. R. (1999). The dynamics of attending: how we track time varying events. *Psychological Review*, 106(1), 119-159